

# Economic Analysis of Technological Processes

## Lecture 5

### Monopoly-Monopoly Behavior-Factor Market-Oligopoly

# Lecture 5: Monopoly

## Market environment:

One company

Setting price or quantity

$r(y) = p(y)y$  denote the revenue function

profit-maximization:

$$\max_y r(y) - c(y)$$

$$MR = MC$$

$$\frac{\Delta r}{\Delta y} = \frac{\Delta c}{\Delta y}$$

$$\Delta r = p\Delta y + y\Delta p$$

$$\frac{\Delta r}{\Delta y} = p + \frac{\Delta p}{\Delta y}y$$

# Lecture 5: Monopoly

$$MR(y) = p(y) \left[ 1 + \frac{1}{\epsilon(y)} \right]$$

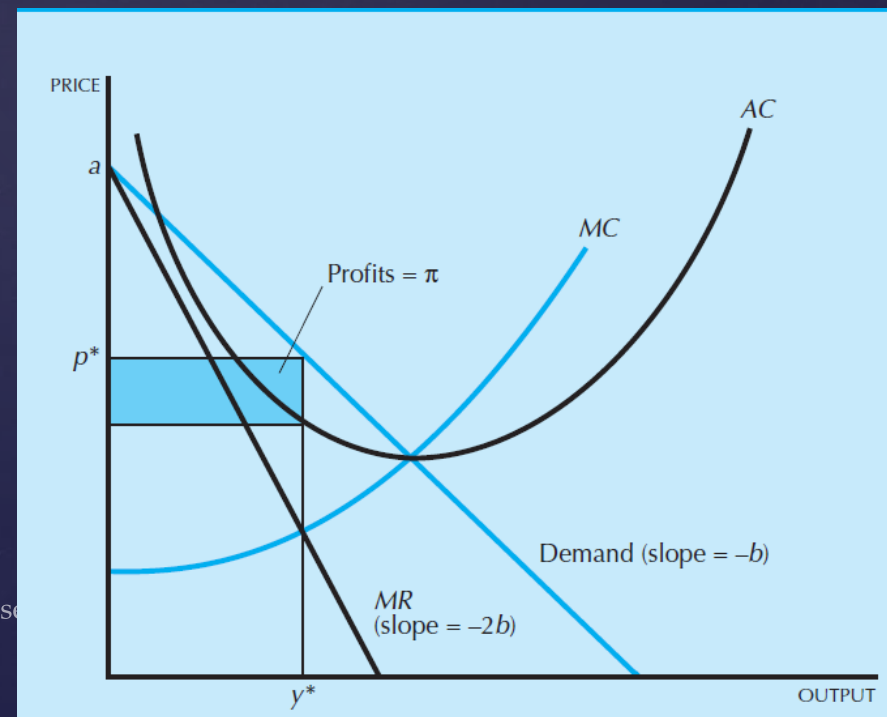
$$p(y) \left[ 1 + \frac{1}{\epsilon(y)} \right] = MC(y)$$

$$p(y) \left[ 1 - \frac{1}{|\epsilon(y)|} \right] = MC(y)$$

$$p(y) = a - by$$

$$r(y) = p(y)y = ay - by^2$$

$$MR(y) = a - 2by$$



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# Lecture 5: Monopoly

## Markup Pricing

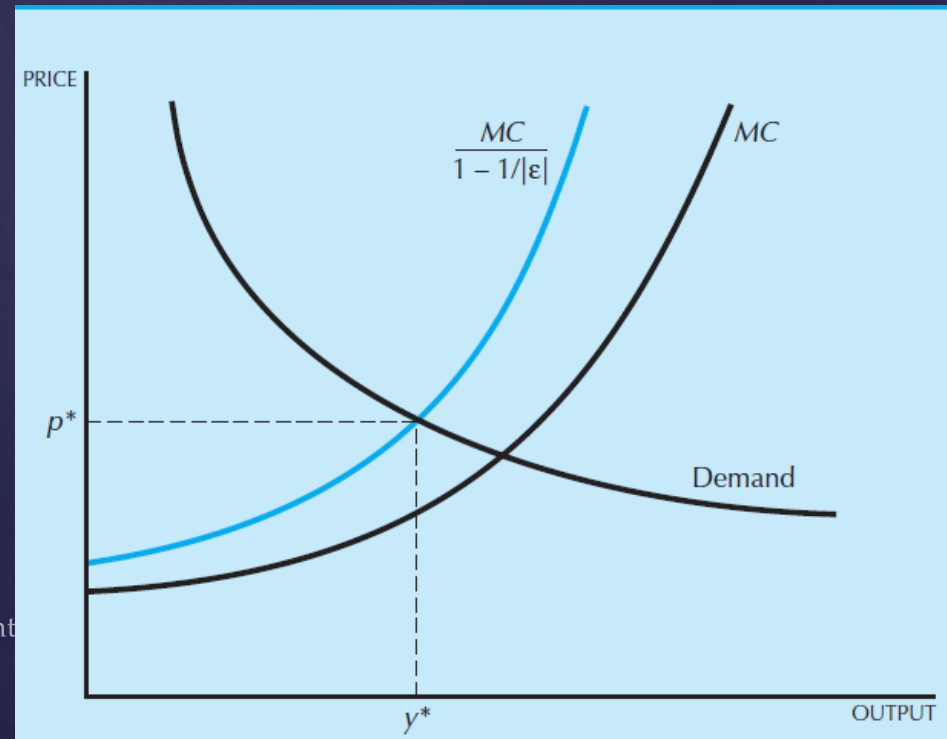
$$p(y) = \frac{MC(y^*)}{1 - 1/|\epsilon(y)|}$$

markup

$$\frac{1}{1 - 1/|\epsilon(y)|}$$

$|\epsilon| > 1$

*Constant*  $p = MC / (1 - 1/|\epsilon|)$



# Lecture 5: Monopoly

## Impact of Tax

$MC+t$

$$a - 2by = c + t$$

$$y = \frac{a - c - t}{2b}$$

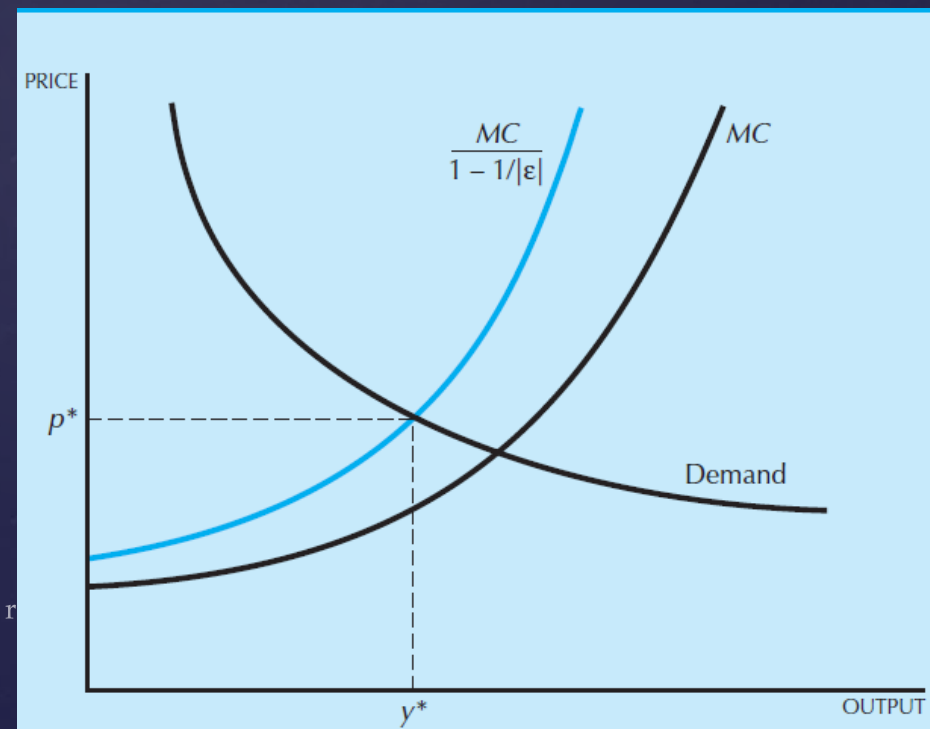
$$\frac{\Delta y}{\Delta t} = -\frac{1}{2b}$$

demand curve

$$p(y) = a - by$$

$$\frac{\Delta p}{\Delta t} = -b \times -\frac{1}{2b} = \frac{1}{2}$$

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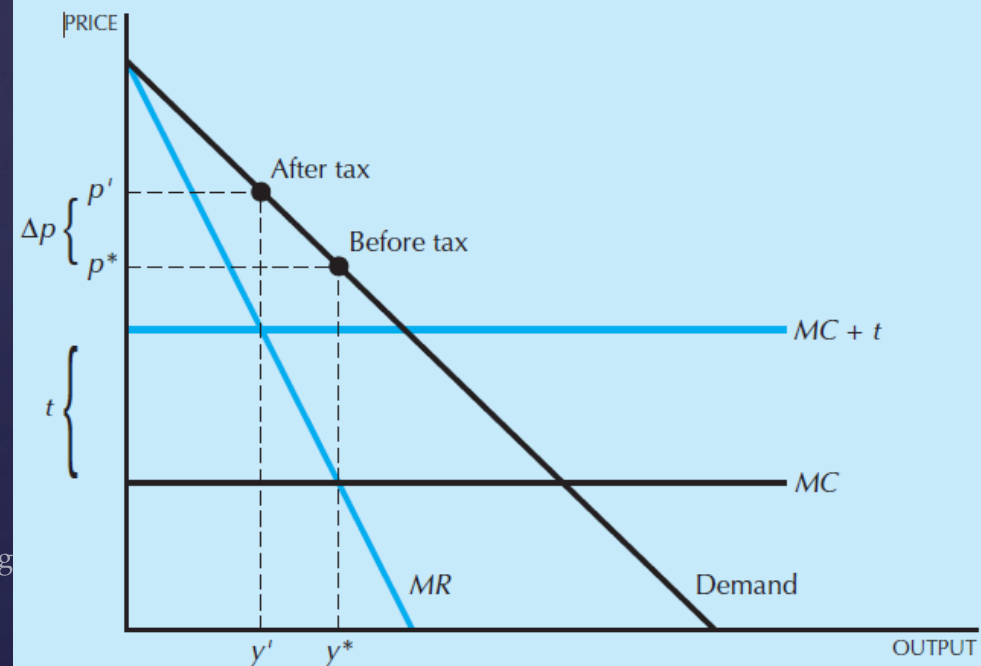
# Lecture 5: Monopoly

$$p = \frac{c + t}{1 - 1/|\epsilon|}$$

$$\frac{\Delta p}{\Delta t} = \frac{1}{1 - 1/|\epsilon|}$$

## profits tax

$$\max_y (1 - \tau)[p(y)y - c(y)]$$



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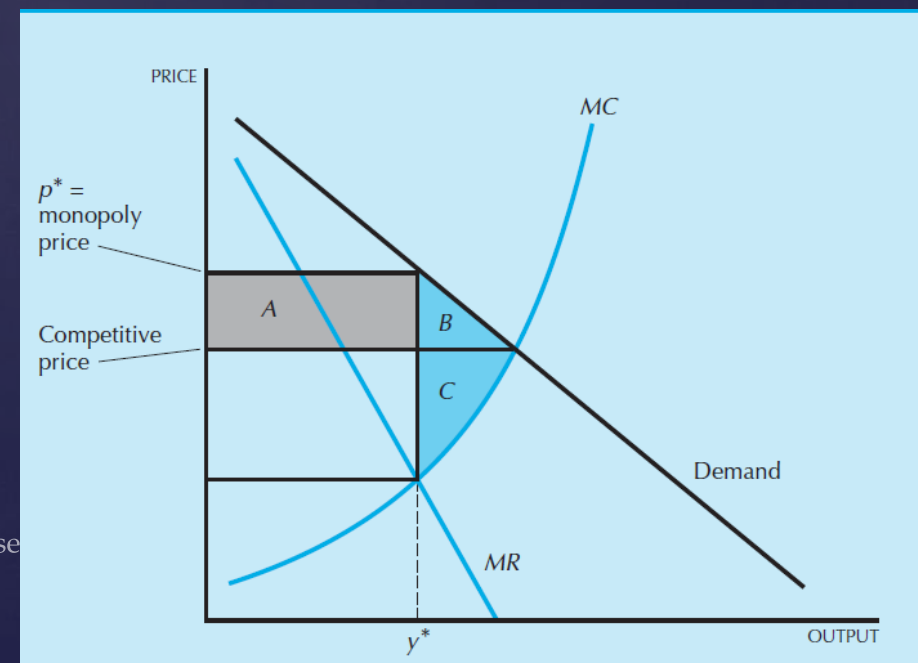
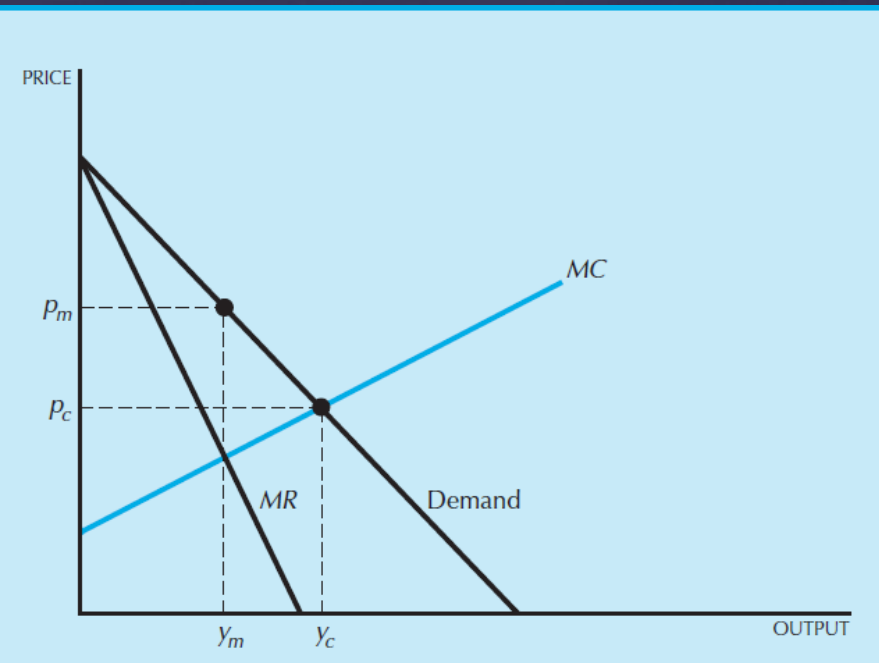
# Lecture 5: Monopoly Inefficiency

relative welfare of consumers and the owners of firms

Pareto efficiency

Deadweight Loss of Monopoly- measure the total loss

Cost of the monopoly



# Lecture 5: Monopoly

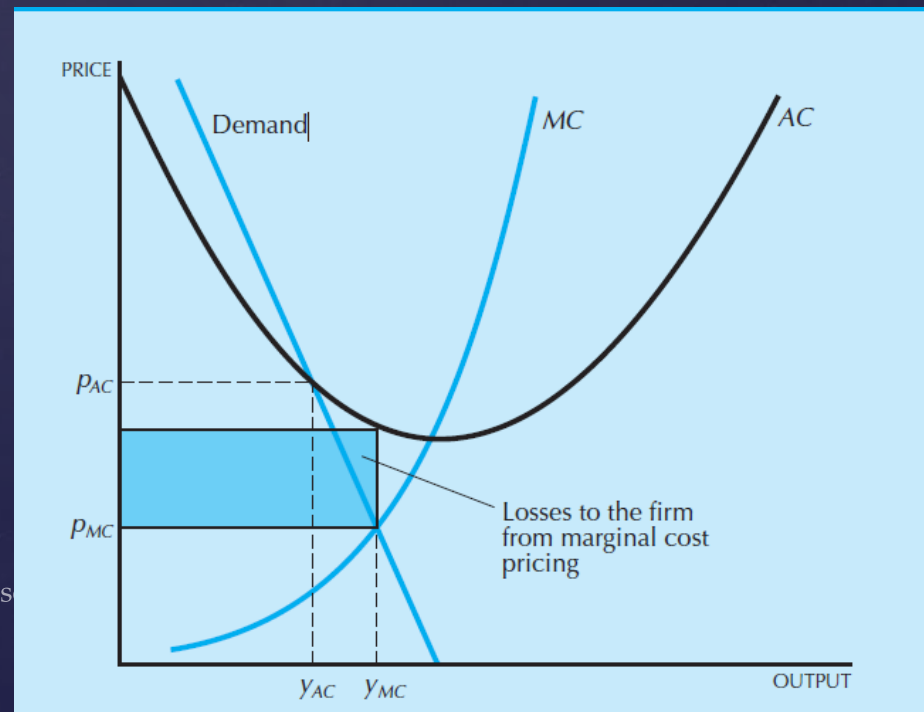
## Natural Monopoly

public utilities: large fixed costs and small variables

regulated or operated by governments

what the true costs of the firm are?

lump-sum subsidy



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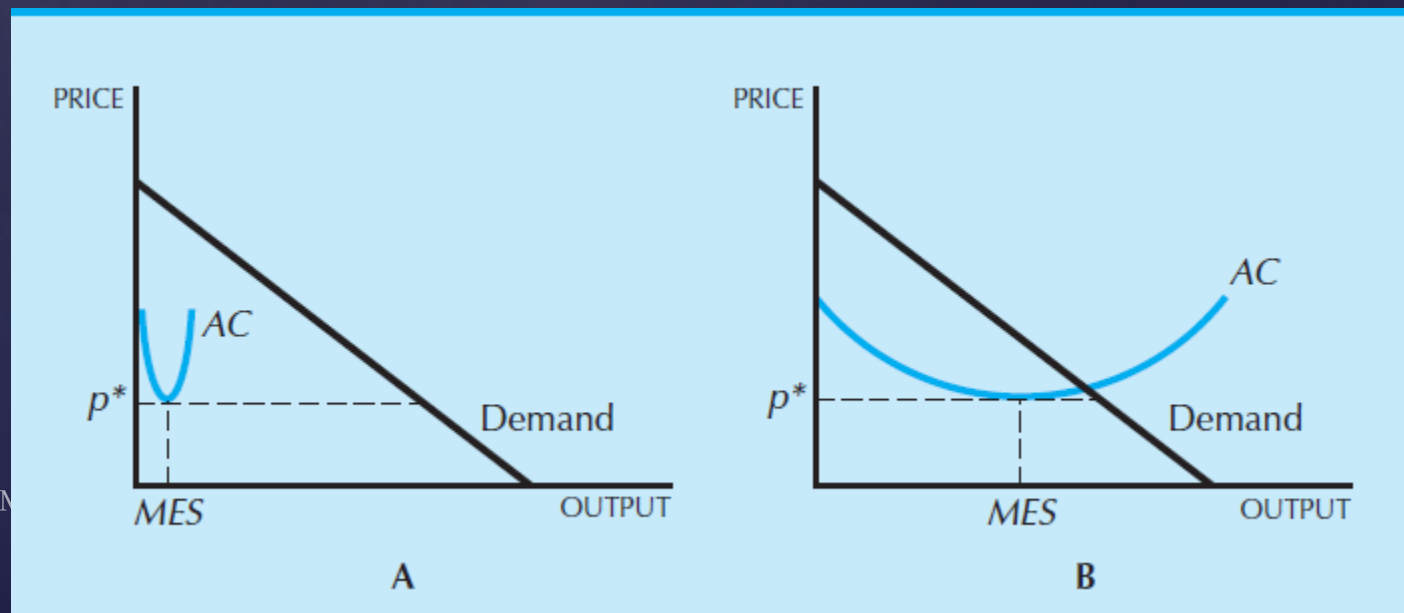
# Lecture 5: Monopoly

## What Causes Monopolies?

size of the minimum efficient scale (MES)

Collusion

Cartel



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# Lecture 5: Monopoly behaviour

some degree of monopoly power

more complicated pricing and marketing strategies

## Price Discrimination

sell different units of output at different prices

First-degree: different prices from person to person

= perfect price discrimination

Second-degree : prices differ across the units of the good, but not across people= bulk discount

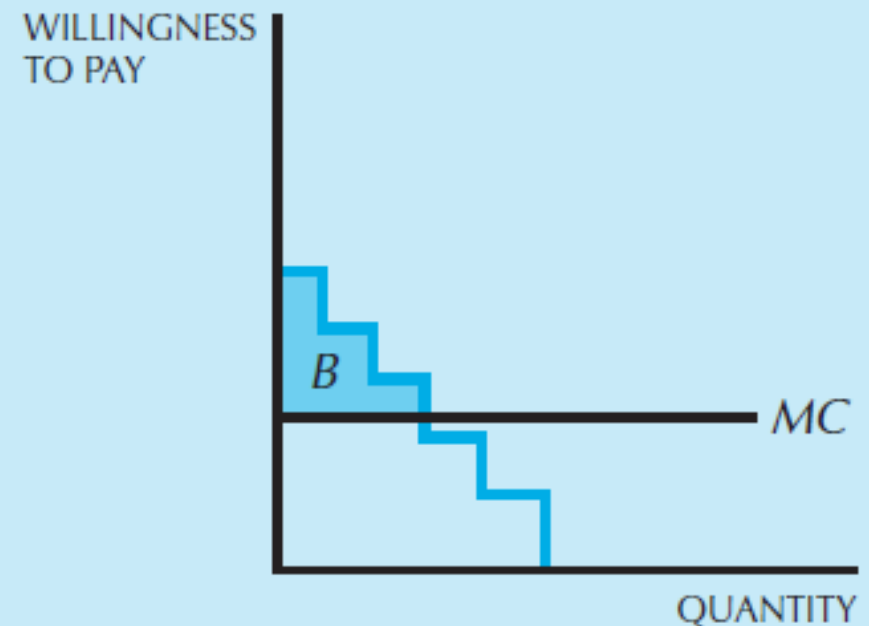
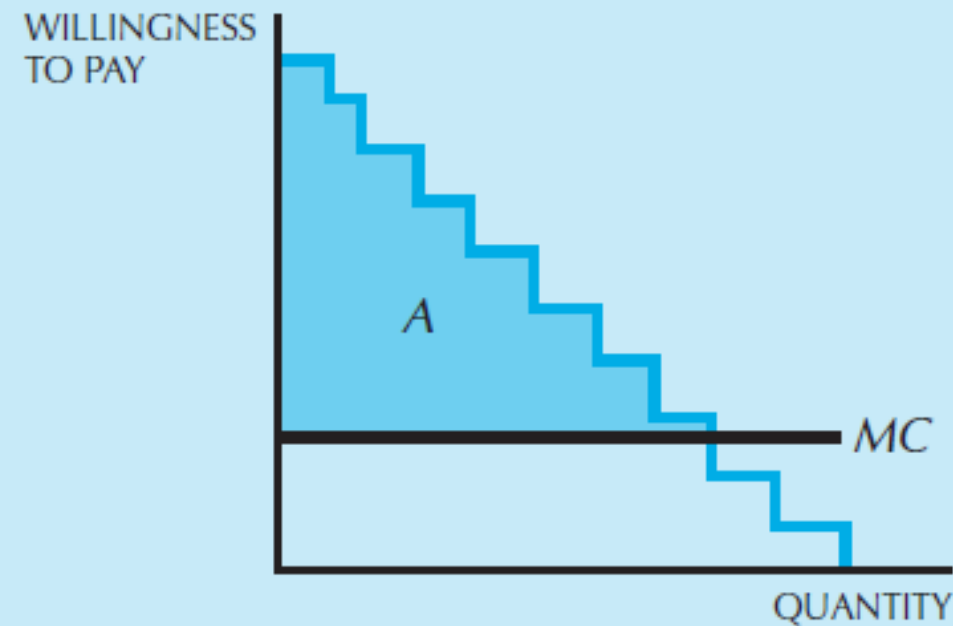
Third-degree: to different people for different prices e.g.  
Senior tickets

# Lecture 5: Monopoly behaviour

## First-Degree Price Discrimination

producer's surplus

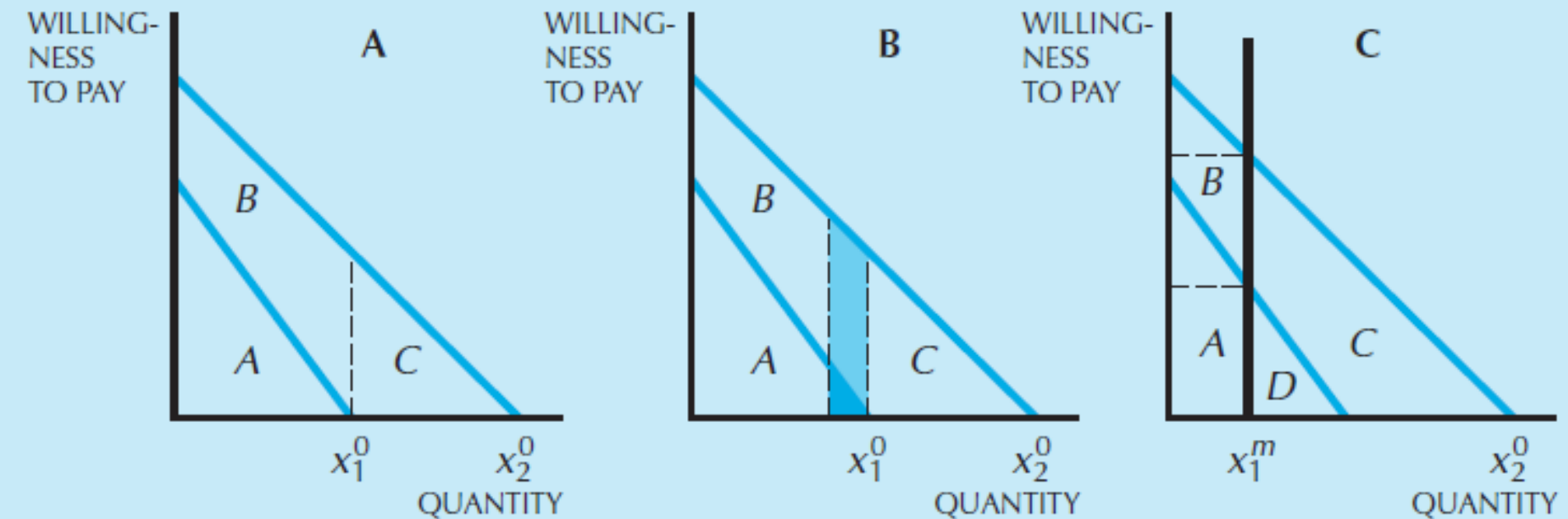
automobile sales or in antique markets



# Lecture 5: Monopoly behaviour

## Second-Degree Price Discrimination

Nonlinear pricing: public utilities, how much is bought



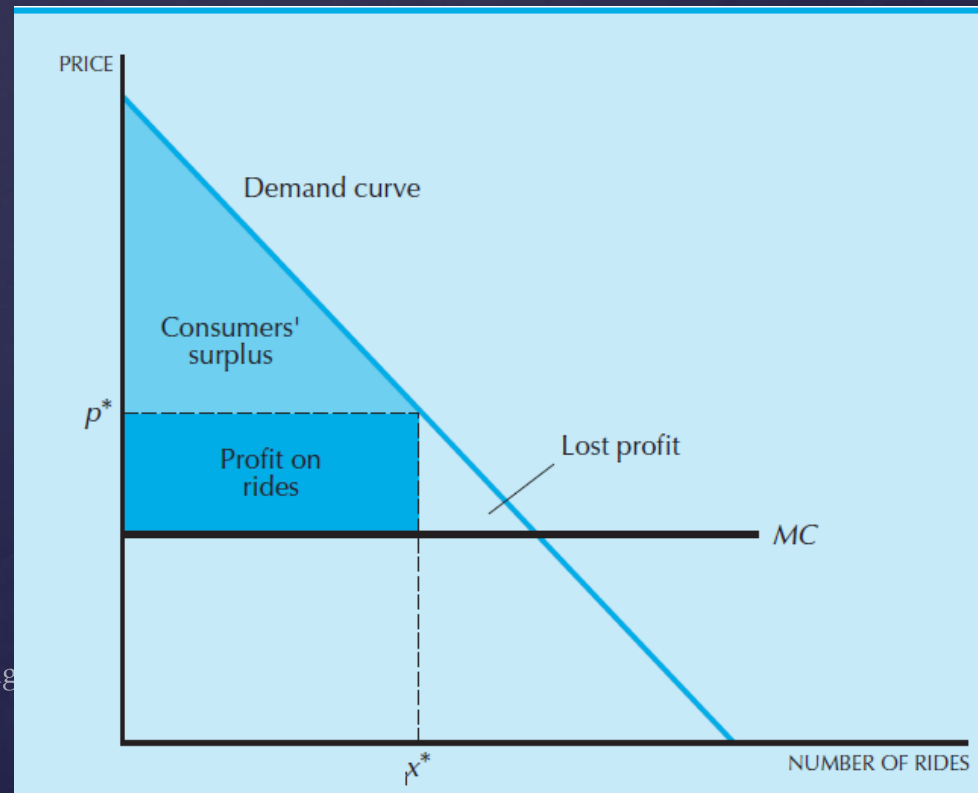
# Lecture 5: Monopoly behaviour

## Third-Degree Price Discrimination

student discounts at the movies, or senior citizens' discounts

Bundling: software suite

Two-Part Tariffs: amusement park



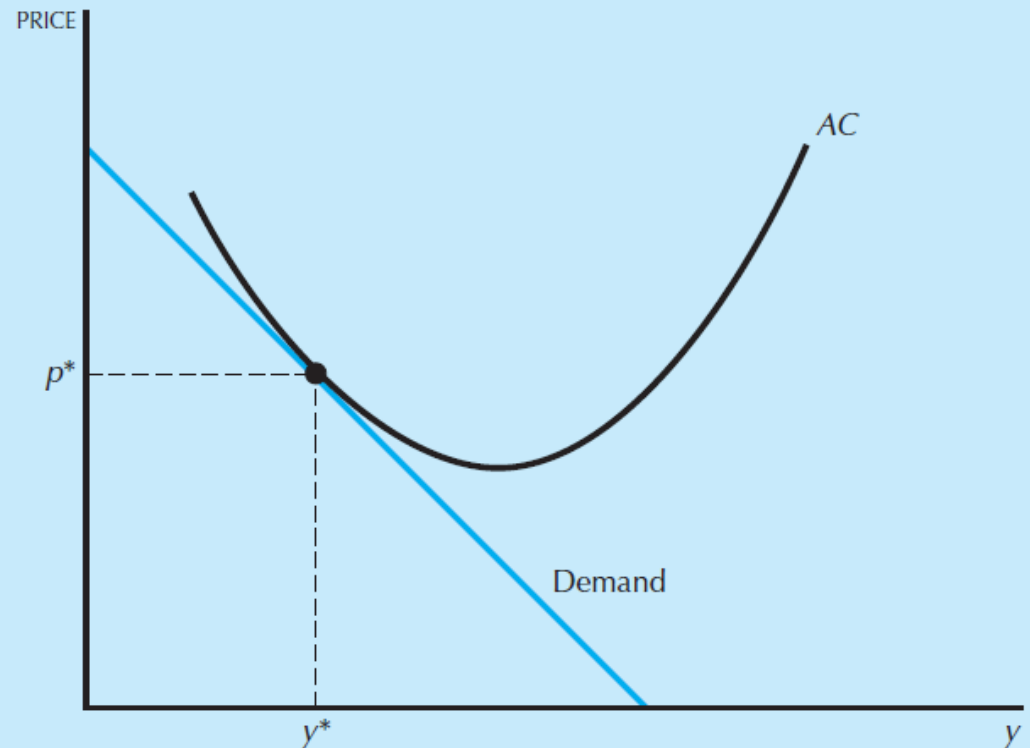
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# Lecture 5: Monopoly behaviour

## Monopolistic Competition (soft drink market)

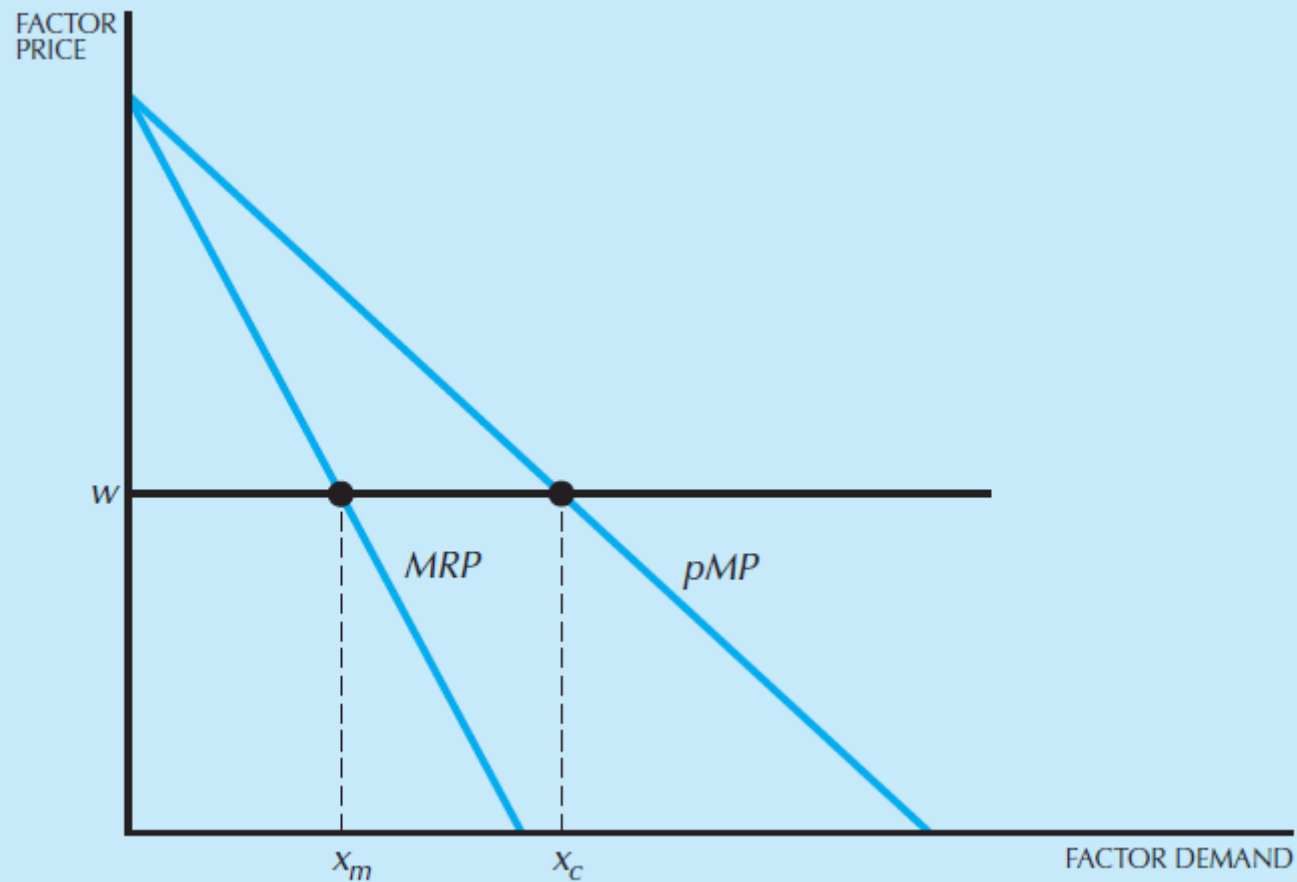
product differentiation

Competition in location



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# Lecture 5: Factor Market



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# Lecture 5: Factor Market

Monopsony: single buyer

Output to be sold in a competitive market

Single input function  $y = f(x)$

price maker

$$\max_x pf(x) - w(x)x$$

$$\Delta c = w\Delta x + x\Delta w$$

$$\frac{\Delta c}{\Delta x} = MC_x = w + \frac{\Delta w}{\Delta x}x$$

$$MC_x = w \left[ 1 + \frac{x}{w} \frac{\Delta w}{\Delta x} \right]$$

$$= w \left[ 1 + \frac{1}{\eta} \right]$$



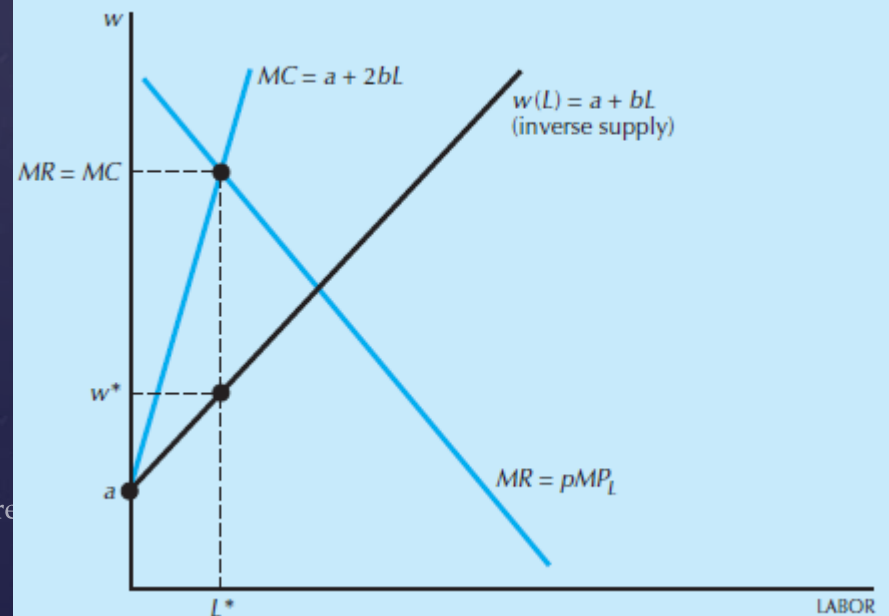
# Lecture 5: Factor Market

Monopsony: single buyer

inverse supply curve:  $w(x) = a + bx$

$$C(x) = w(x)x = ax + bx^2$$

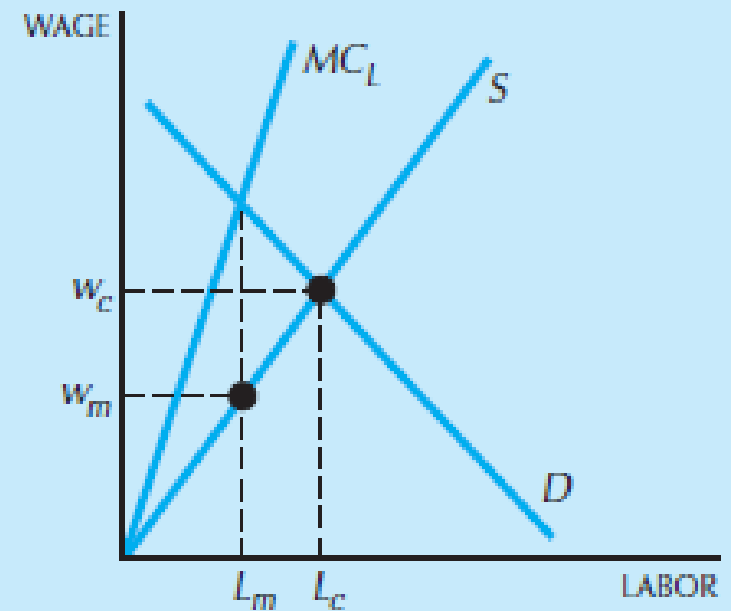
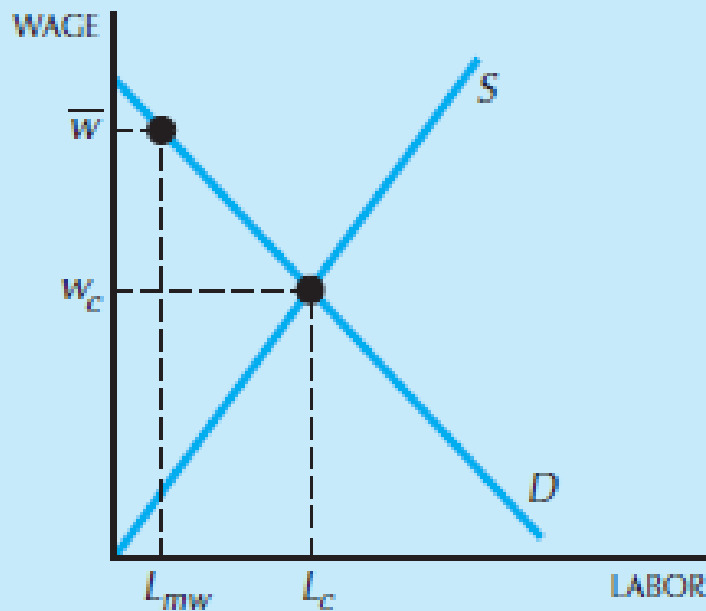
$$MC_x(x) = a + 2bx$$



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# Lecture 5: Factor Market

## Minimum wage



Some parts

# Lecture 5: Oligopoly

Number of competitors in the market, but not so many

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negligible effect on price

strategic interactions in an industry with a small number of firms.

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Duopoly, identical product

sequential game: leader and follower in price/quantity

simultaneous game: not considering the other's decisions

to collude: cooperative game

# Lecture 5: Oligopoly

## Pricing Matching (Tires):

a vendor that offers a low-price guarantee takes away much of its competitors' motivation for cutting prices

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## Quantity Leadership= Stackelberg model:

dominant firm, or a natural leader: IBM

Output:  $Y = y_1 + y_2$

The Follower's Problem:  $\max_{y_2} p(y_1 + y_2)y_2 - c_2(y_2)$

$$MR_2 = p(y_1 + y_2) + \frac{\Delta p}{\Delta y_2}y_2 = MC_2$$

# Lecture 5: Oligopoly

Reaction function:

$$y_2 = f_2(y_1)$$

Linear demand, inverse function:

$$p(y_1 + y_2) = a - b(y_1 + y_2)$$

0 cost, profit function:

$$\pi_2(y_1, y_2) = [a - b(y_1 + y_2)]y_2$$

isoprofit lines

$$ay_2 - by_1y_2 - by_2^2 = \bar{\pi}_2$$

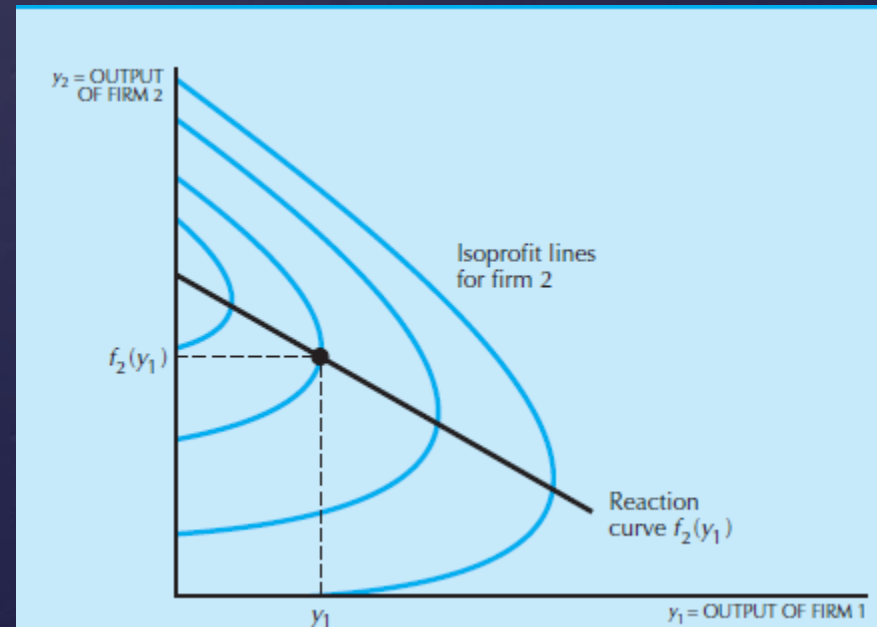
$$MR_2(y_1, y_2) = a - by_1 - 2by_2$$

MR=MC and MC=0

$$a - by_1 - 2by_2 = 0$$

Reaction curve, company 2:

$$y_2 = \frac{a - by_1}{2b}$$



# Lecture 5: Oligopoly

## The Leader's Problem:

$$\max_{y_1} p(y_1 + y_2)y_1 - c_1(y_1)$$

$$y_2 = f_2(y_1)$$

$$\max_{y_1} p[y_1 + f_2(y_1)]y_1 - c_1(y_1)$$

$$f_2(y_1) = y_2 = \frac{a - by_1}{2b}$$

$$\pi_1(y_1, y_2) = p(y_1 + y_2)y_1 = ay_1 - by_1^2 - by_1y_2$$

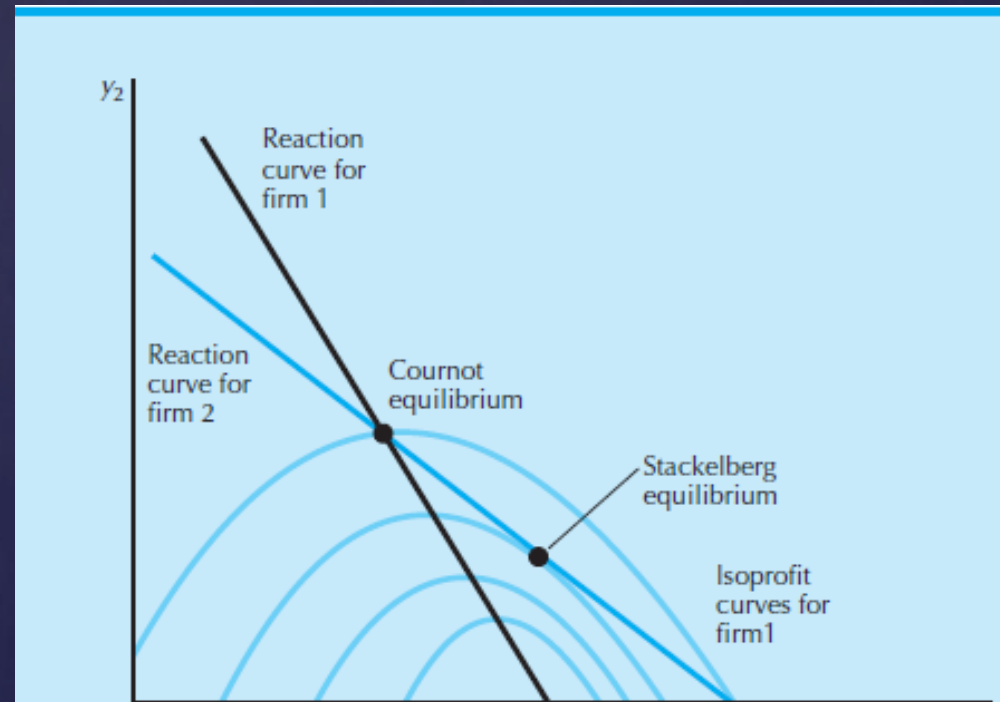
$$\pi_1(y_1, y_2) = \frac{a}{2}y_1 - \frac{b}{2}y_1^2$$

$$MR = \frac{a}{2} - by_1$$

$$y_1^* = \frac{a}{2b}$$

$$y_2^* = \frac{a - by_1^*}{2b}$$

$$= \frac{a}{4b}$$



# Lecture 5: Oligopoly

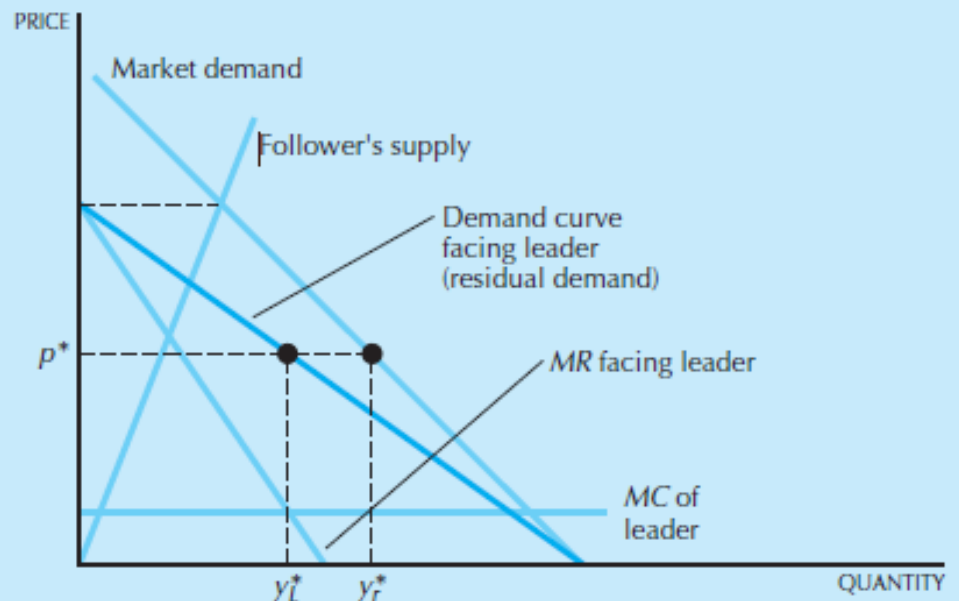
Price Leadership:

Follower's behaviour:

residual demand curve

$$\max_{y_2} py_2 - c_2(y_2)$$

$$\pi_1(p) = (p - c)[D(p) - S(p)] = (p - c)R(p)$$



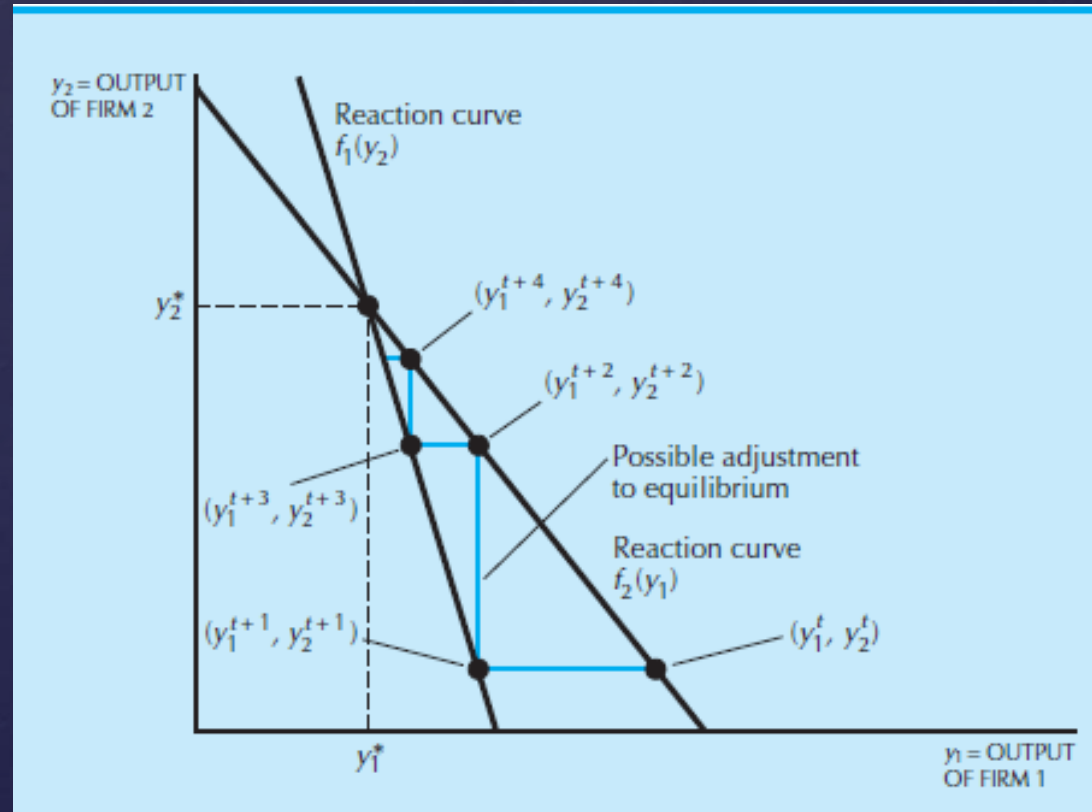
# Lecture 5: Oligopoly

## Comparing Price Leadership and Quantity Leadership

### Simultaneous Quantity Setting= Cournot model

stable equilibrium

Many firms in  
Cournot equilibrium





# Lecture 5: Oligopoly

## Collusion

## Cartel

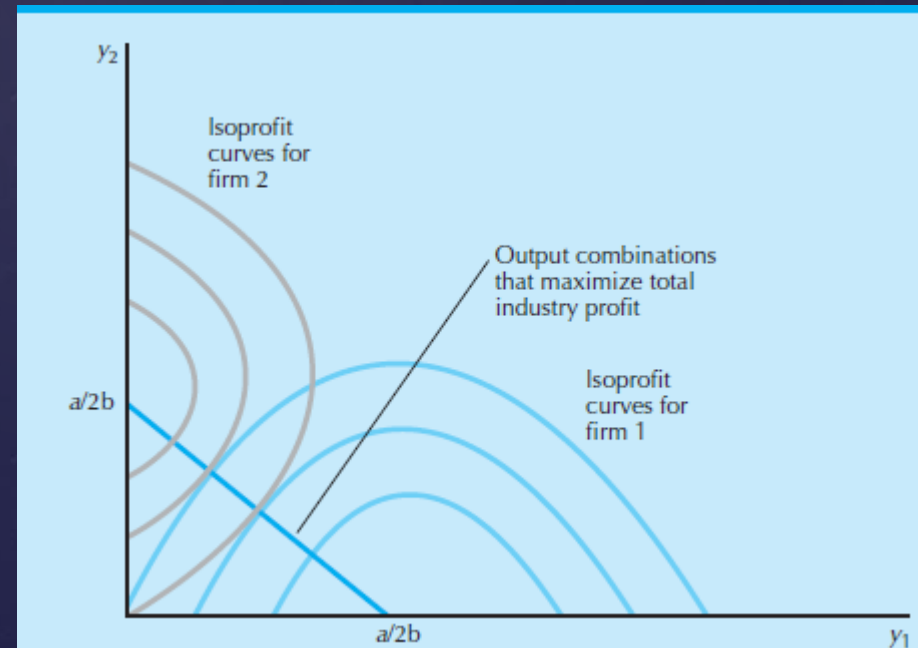
firms act together to restrict output so as not to “spoil” the market

detect and punish cheating

$$\pi(y_1, y_2) = [a - b(y_1 + y_2)](y_1 + y_2) = a(y_1 + y_2) - b(y_1 + y_2)^2$$

$$a - 2b(y_1^* + y_2^*) = 0$$

$$y_1^* + y_2^* = \frac{a}{2b}$$



# Lecture 5: Oligopoly

## Punishment Strategies and the size of them

$$\text{Present value of cartel behavior} = \pi_m + \frac{\pi_m}{r}$$

$$\text{Present value of cheating} = \pi_d + \frac{\pi_c}{r}$$

$$\pi_m + \frac{\pi_m}{r} > \pi_d + \frac{\pi_c}{r}$$

$$r < \frac{\pi_m - \pi_c}{\pi_d - \pi_m}$$